

About Electron Position in Ground State of Hydrogen Atom

(Another Variation on a Theme)

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Abstract: In this paper according to Heracleitean dynamics the electron radial position in the ground state of Hydrogen atom is introduced, i.e. $r_{1,2} = R_{Bohr} \mp 1.226301\lambda_{Compton}$ of the electron.

Keywords: Heracleitean dynamics and electron radial position in the ground state of Hydrogen atom, pseudo-Heracleitean dynamics on double surface and electron position radius

1. PREFACE

The subject of interest of this paper is with the help of Heracleitean dynamics[1]to enlighten the electron position in the ground state of Hydrogen atom.

2. THE GROUND CIRCUMSTANCES

At Heracleitean dynamics [1] mass particles possess zero kinetic energy at the non-zero speed. It happens at the ground circumstances where mass, denoted m_{ground} , and speed, denoted v_{ground} , is related by the dynamic constant k as follows[1]:

$$m_{ground} \times v_{ground} = \sqrt{k}. \quad (1)$$

For the purpose of the present paper it is convenient to express the speed in the units of official speed of light c as:

$$a_{ground} = \frac{v_{ground}}{c}. \quad (2)$$

Hence(1), (2):

$$m_{ground} \times a_{ground} = \frac{\sqrt{k}}{c}. \quad (3)$$

3. THE ELECTRON GROUND CIRCUMSTANCES

Taking into account $k = 6.2723515 \times 10^{-46} kg^2 m^2 s^{-2}$ [2] and $c = 2.99792458 \times 10^8 \frac{m}{s}$ [3] the electron with the ground mass $m_{ground} = 9,109 382 15(45) \times 10^{-31} kg$ [3]has the next ground speed expressed in the units of official speed of light c :

$$a_{ground} = \frac{v_{ground}}{c} = 0,091707650973. \quad (4)$$

4. THE GROUND STATE OF HYDROGEN ATOM

In the ground state of Hydrogen atom the electron possesses the non-zero kinetic energy $W_k = \Delta m c^2$. The concerned non-zero mass equivalent Δm is related to the inverse fine structure constant α^{-1} [4]:

$$\Delta m = \frac{m_{ground}}{2\alpha^{-2}}. \quad (5)$$

Applying (5) is evident that the electron non-ground mass m is related to the inverse fine structure, too:

$$m = m_{ground} + \Delta m = m_{ground} \left(1 + \frac{1}{2\alpha^{-2}} \right). \quad (6)$$

Two different speeds $a_1 < a_{ground}$ and $a_2 > a_{ground}$ belong to the non-ground mass m of the electron in the ground state of Hydrogen atom[1]:

$$a_1 \times a_2 = \frac{k}{m^2 c^2}. \tag{7}$$

The above speeds are given solving the pantarei equation[1]:

$$m^2 c^2 a^2 = e^{\frac{m_{ground}^2 c^2 - k(1 - \ln k) + m^2 c^2 (a^2 - 1)}{k}}. \tag{8}$$

For the theoretical inverse fine structure constant $\alpha^{-1} = 137.036006$ deduced from the double surface concept[5], for instance, the electron non-ground speeds a_1 and a_2 in the ground state of Hydrogen atom are the next:

$$a_1 = 0.086594611656 < a_{ground} = 0.091707650973 < a_2 = 0.096912605053. \tag{9}$$

And the average electron speed \bar{a} in that state yields:

$$\bar{a} = \frac{a_1 + a_2}{2} = 0.091753608354 = 1,000501129200 a_{ground}. \tag{10}$$

5. THE ELECTRON PATH IN THE GROUND STATE OF HYDROGEN ATOM

In the ground state of Hydrogen atom the electron circulates with the average speed \bar{a} (10) on Bohr circumference of the length $\bar{s} = \alpha^{-1}$ expressed in Compton wavelengths of the electron[6]. With the lower speed a_1 the electron circulates below and with the higher speed a_2 above that average orbit. To pass the different circulation paths s in the same time t the ratio of paths s should equal the ratio of speeds a :

$$t = \frac{s_1}{a_1} = \frac{\bar{s}}{\bar{a}} = \frac{s_2}{a_2}. \tag{12}$$

Hence:

$$\frac{s_1}{\bar{s}} = \frac{a_1}{\bar{a}} \quad \text{and} \quad \frac{s_1}{s_2} = \frac{a_1}{a_2} \quad \text{and} \quad \frac{s_2}{\bar{s}} = \frac{a_2}{\bar{a}}. \tag{13}$$

The same holds true for the corresponding circulation radii $r = \frac{s}{2\pi}$:

$$\frac{r_1}{R_{Bohr}} = \frac{a_1}{\bar{a}} \quad \text{and} \quad \frac{r_1}{r_2} = \frac{a_1}{a_2} \quad \text{and} \quad \frac{r_2}{R_{Bohr}} = \frac{a_2}{\bar{a}}. \tag{14}$$

Using the relations (13) and (14) the circulation circumferences and corresponding radii can be calculated. The mentioned data are collected in the Table 1.

Table 1. The electron speeds, circumferences and corresponding radii in the ground state of Hydrogen atom

	Circulation speed (c)	Circulation circumference ($\lambda_{Compton}$)	Circulation radius ($\lambda_{Compton}$)
Higher position	$a_2 = 0.096912605053$	$s_2 = 144.741080 = \alpha^{-1} + 7.705074$	$r_2 = 23.036258 = R_{Bohr} + 1.226301$
Average position	$\bar{a} = 0.091753608354$	$\bar{s} = 137.036006 = \alpha^{-1}$	$\bar{r} = 21,809958 = R_{Bohr}$
Lower position	$a_1 = 0.086594611656$	$s_1 = 129.330932 = \alpha^{-1} - 7.705074$	$r_1 = 20.583657 = R_{Bohr} - 1.226301$
Extreme difference	$\Delta a = a_2 - a_1 = 0.010317993397$	$\Delta s = s_2 - s_1 = 15.410148$	$\Delta r = r_2 - r_1 = 2.452602$

It is evident from the Table 1 that the proposed higher and lower electron position in the ground state of Hydrogen atom is found at 1.226301 Compton wavelengths of the electron apart from Bohr radius. And the radial distance between both extreme electron positions Δr is the next:

$$\Delta r = r_2 - r_1 = 2.452602 \lambda_{Compton}. \tag{15}$$

Following pseudo-Heraclitean dynamics on double surface the electron should be found somewhere on its position radius $r_{position} = 2.487435$ expressed in Compton wavelengths of the electron[7] what is in accordance with the given result(15):

$$\Delta r = 2.452602 \lambda_{Compton} < r_{position} = 2.487435 \times \lambda_{Compton}. \tag{16}$$

6. CONCLUSIONS

The proposed extreme radial distance between the electron positions in the ground state of Hydrogen atom Δr is a consequence of Heracleatean dynamics. On the other hand the electron position radius $r_{position}$ is a consequence of pseudo-Heracleatean dynamics. The observed similarity of numbers shows the common essence of both aspects of the theory.

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